

An Incremental Approach to Structured Argumentation over Dynamic Knowledge Bases

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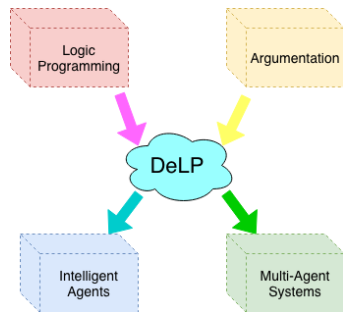
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Dynamic Structured Argumentation

- Argumentation frameworks are often dynamic (change over time) as a consequence of the fact that argumentation is inherently dynamic (change mind/opinion, new available knowledge)
- We focus on **Defeasible Logic Programming**, a formalism that combines results of Logic Programming and Defeasible Argumentation.
- We devise an incremental technique for computing conclusions in structured argumentation frameworks (avoiding wasted effort due to recomputation from scratch)



Outline

- 1 Introduction
 - Motivation
- 2 Background
 - Defeasible Logic Programming
- 3 Complexity Analysis
 - Complexity Results
- 4 Incremental Computation
 - Updates
 - Dealing with Irrelevant Updates
 - Dealing with Relevant Updates
 - Our Technique
- 5 Implementation & Experiments
- 6 Conclusions & Future Work

A DeLP Program

DeLP considers two kinds of program rules:

- **Defeasible** rules to represent tentative information, and
- **Strict** rules used to represent strict knowledge.

Example (A DeLP-program \mathcal{P}_1)

Consider the DeLP-program $\mathcal{P}_1 = (\Pi_1, \Delta_1)$, where:

$$\Pi_1 = \{ \sim a, t, b, (d \leftarrow t) \}$$

$$\Delta_1 = \left\{ \begin{array}{lll} (i \leftarrow s), & (s \leftarrow h), & (h \leftarrow b), \\ (\sim h \leftarrow d, t), & (\sim i \leftarrow \sim a, s), & (a \leftarrow t), \\ (s \leftarrow d), & (h \leftarrow d), & (\sim f \leftarrow \sim e), \\ (\sim e \leftarrow \sim h, \sim a) & & \end{array} \right\}$$

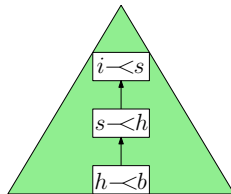
Argument

Given a DeLP program $\mathcal{P} = (\Pi, \Delta)$ and a literal α , we say that $\langle \mathcal{A}, \alpha \rangle$ is an argument for α if \mathcal{A} is a set of defeasible rules of Δ such that:

- (i) there is a derivation for α from $\Pi \cup \mathcal{A}$,
- (ii) the set $\Pi \cup \mathcal{A}$ is not contradictory, and
- (iii) \mathcal{A} is minimal (i.e., there is no proper subset \mathcal{A}' of \mathcal{A} satisfying both (i) and (ii)).

Example (An argument for \mathcal{P}_1)

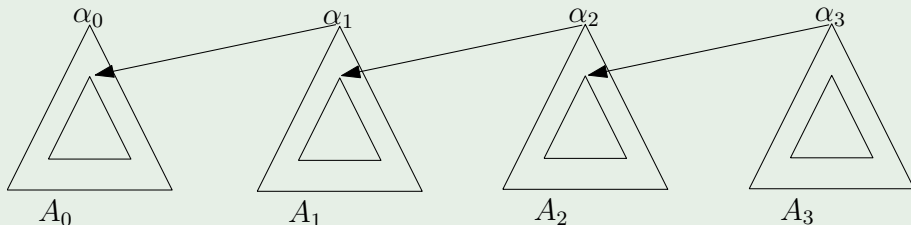
- $\langle \mathcal{A}_1, i \rangle = \langle \{(i \prec s), (s \prec h), (h \prec b)\}, i \rangle$



Argumentation Line

- A sequence of arguments obtained from a DeLP program, where each element of the sequence is a **defeater** of its predecessor.

Example (Argumentation Line)



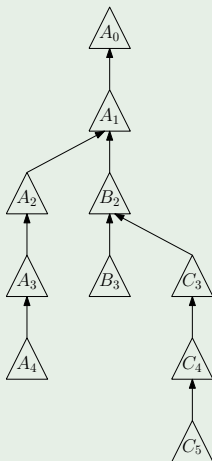
Example (An argumentation line for \mathcal{P}_1)

Given the two arguments: $\langle \mathcal{A}_1, i \rangle = \langle \{(i \multimap s), (s \multimap h), (h \multimap b)\}, i \rangle$, and
 $\langle \mathcal{A}_2, \sim i \rangle = \langle \{(\sim i \multimap \sim a, s), (s \multimap d)\}, \sim i \rangle$
 an argumentation line is the following: $[\mathcal{A}_1, \mathcal{A}_2]$

Dialectical Process

- Given an argument A for a literal L , the dialectical tree contains all acceptable argumentation lines that start with that argument.
- It allows to determine the status for a given argument.

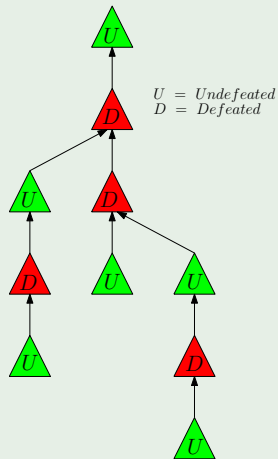
Example (Dialectical Tree)



Dialectical Process

- All leaves are marked as **Undeclared**.
- An argument in the tree is marked as **Defeated** if and only if it has at least a child marked as **Undeclared**.

Example (Dialectical Tree)



Status of literals

The status of literals allow us to determine the conclusions we can draw from a DeLP-program.

$S_{\mathcal{P}} : Lit \rightarrow \{\text{IN}, \text{OUT}, \text{UNDECIDED}, \text{UNKNOWN}\}$ assigning a *status* to each literal w.r.t. \mathcal{P} as follows:

- $S_{\mathcal{P}}(\alpha) = \text{IN}$ if there exists a (marked) dialectical tree whose root α is *Undefeated*
- $S_{\mathcal{P}}(\alpha) = \text{OUT}$ if $S_{\mathcal{P}}(\sim\alpha) = \text{IN}$
- $S_{\mathcal{P}}(\alpha) = \text{UNDECIDED}$ if neither $S_{\mathcal{P}}(\alpha) = \text{IN}$ nor $S_{\mathcal{P}}(\alpha) = \text{OUT}$
- $S_{\mathcal{P}}(\alpha) = \text{UNKNOWN}$ if $\alpha \notin Lit_{\mathcal{P}}$, i.e., α is not in the language of the program

Example (Arguments from the previous program)

Given \mathcal{P} , then $S_{\mathcal{P}_1}(h) = \text{IN}$, $S_{\mathcal{P}_1}(a) = \text{OUT}$, and $S_{\mathcal{P}_1}(i) = \text{UNDECIDED}$.

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Theorem Given \mathcal{P} and a literal $\alpha \in Lit_{\mathcal{P}}$, deciding whether there is an argument for α w.r.t. \mathcal{P} is NP-complete.

Corollary Let $\mathcal{P} = (\Pi, \Delta)$ be a DeLP-program such that for all $r \in (\Pi \cup \Delta)$, $|body(r)| \leq 2$. Deciding whether there is an argument for $\alpha \in Lit_{\mathcal{P}}$ w.r.t. \mathcal{P} is NP-complete.

Proposition Given $\mathcal{P} = (\Pi, \Delta)$ and a literal $\alpha \in Lit_{\mathcal{P}}$, deciding whether there is an argument for α w.r.t. \mathcal{P} is in PTIME if either (i) α does not depend in $G(\mathcal{P})$ on literals β and γ such that $\{\beta, \gamma\} \cup \Pi$ is contradictory, or (ii) α is not in $G(\mathcal{P})$.

Corollary Let $\mathcal{P} = (\Pi, \Delta)$ be a DeLP-program such that for all $r \in (\Pi \cup \Delta)$, $|body(r)| \leq 2$. Deciding whether $S_{\mathcal{P}}(\alpha) = \text{IN}$, $S_{\mathcal{P}}(\alpha) = \text{OUT}$, or $S_{\mathcal{P}}(\alpha) = \text{UNDECIDED}$, for $\alpha \in Lit_{\mathcal{P}}$ is NP-hard.

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Updating a DeLP program

- An update consists of modifying a DeLP-program \mathcal{P} into a new DeLP-program \mathcal{P}' by adding or removing a strict or a defeasible rule.

Example (Perform $u = +(\sim i \prec h)$ on \mathcal{P}_1)

The updated DeLP-program $\mathcal{P}'_1 = (\Pi'_1, \Delta'_1)$, is as follows:

$$\Delta'_1 = \Delta_1 = \left\{ \begin{array}{lll} \Pi'_1 = \Pi_1 = \{ \sim a, t, b, (d \leftarrow t) \} \\ (i \prec s), & (s \prec h), & (h \prec b), \\ (\sim h \prec d, t), & (\sim i \prec \sim a, s), & (a \prec t), \\ (s \prec d), & (h \prec d), & (\sim f \prec \sim e), \\ (\sim e \prec \sim h, \sim a) \end{array} \right\} \cup \{(\sim i \prec h)\}$$

- If r is a strict rule and $u = +r$, then $\mathcal{P}' = ((\Pi \cup \{r\}), \Delta)$ if $(\Pi \cup \{r\})$ is guaranteed to be not contradictory, otherwise $\mathcal{P}' = \mathcal{P}$.

Question

- After performing an update the conclusion that can be derived may change.

Should we recompute the status of literals from scratch?

- The fact that computing the status of arguments is hard motivated the investigation of incremental techniques.

Overview of our incremental approach

Two main steps:

- 1) First, we check if the update is *irrelevant* (the status of all literals are preserved). In such a case we simply return the initial status $S_{\mathcal{P}}$.
- 2) To efficiently deal with *relevant* updates, we identify the subset of literals whose status needs to be recomputed after performing an update, and only recompute their status.

Hyper-graph for a DeLP-Program

Given a program \mathcal{P} , $G(\mathcal{P}) = \langle N, H \rangle$ is defined as follows:

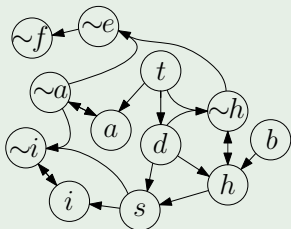
- If there is a strict derivation in Π for literal α , then $\alpha \in N$;
- For each strict rule $\alpha_0 \leftarrow \alpha_1, \dots, \alpha_n$ (resp., defeasible rule $\alpha_0 \prec \alpha_1, \dots, \alpha_n$) such that $\alpha_1, \dots, \alpha_n \in N$, then $\alpha_0 \in N$ and $(\{\alpha_1, \dots, \alpha_n\}, \alpha_0) \in H$;
- For each pair of nodes in N representing complementary literals α and $\sim\alpha$, both $(\{\alpha\}, \sim\alpha) \in H$ and $(\{\sim\alpha\}, \alpha) \in H$.

Example (Hyper-graph $G(\mathcal{P}_1)$ for \mathcal{P}_1)

Consider the DeLP-program $\mathcal{P}_1 = (\Pi_1, \Delta_1)$, where:

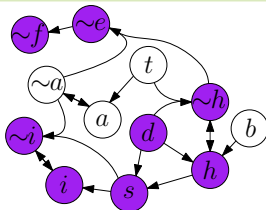
$$\Pi_1 = \{\sim a, t, b, (d \leftarrow t)\}$$

$$\Delta_1 = \left\{ \begin{array}{lll} (i \prec s), & (s \prec h), & (h \prec b), \\ (\sim h \prec d, t), & (\sim i \prec \sim a, s), & (a \prec t), \\ (s \prec d), & (h \prec d), & (\sim f \prec \sim e), \\ (\sim e \prec \sim h, \sim a) & & \end{array} \right\}$$



Reachable and Preserved Literals

- We say that a node y is *reachable* from a set X of nodes if there exists a hyper-path from X to y .
- We use $Reach_{G(\mathcal{P})}(X)$ to denote the set of all nodes that are reachable from X in $G(\mathcal{P})$.
- $Reach_{G(\mathcal{P}_1)}(\{d\}) = \{d, h, \sim h, s, \sim i, i, \sim e, \sim f\}$



Lemma (1) (Preserved literals)

Let \mathcal{P} be a DeLP-program, $u = \pm r$ an update for \mathcal{P} , and $\mathcal{R}(u, \mathcal{P}) = Reach_{G(u, \mathcal{P})}(\{head(r)\})$. Let $\mathcal{P}' = u(\mathcal{P})$ be the updated program, and $G(\mathcal{P}') = \langle N', H' \rangle$ be the updated hyper-graph. Then, a literal $\alpha \in N'$ is preserved (i.e., $S_{\mathcal{P}}(\alpha) = S_{\mathcal{P}'}(\alpha)$) if $\alpha \notin \mathcal{R}(u, \mathcal{P})$.

- If a literal is not reachable in the hyper-graph, then its status does not change after the update.

Irrelevant updates

Proposition (2) Status of the head of the rule)

Let \mathcal{P} be a DeLP-program and $r = \alpha_0 \prec \alpha_1, \dots, \alpha_n$ a **defeasible** rule such that $\{\alpha_0, \dots, \alpha_n\} \subseteq (\text{Lit}_{\mathcal{P}} \cap \text{Lit}_{\mathcal{P}'})$.

(1) If $S_{\mathcal{P}}(\alpha_0) = \text{IN}$ then $+r$ is irrelevant for \mathcal{P} .

(2) If $S_{\mathcal{P}}(\alpha_0) = \text{OUT}$ then $-r$ is irrelevant for \mathcal{P} .

Proposition (3) Belonging to the Hyper-Graph)

Let \mathcal{P} be a DeLP-program and r a **strict** rule $\alpha_0 \leftarrow \alpha_1, \dots, \alpha_n$ or **defeasible** rule $\alpha_0 \prec \alpha_1, \dots, \alpha_n$ such that $\{\alpha_0, \dots, \alpha_n\} \subseteq (\text{Lit}_{\mathcal{P}} \cap \text{Lit}_{\mathcal{P}'})$. Update $u = \pm r$ is irrelevant for \mathcal{P} if α_0 does not belong to $G(u, \mathcal{P})$.

Proposition (4) Reachable in the Hyper-Graph)

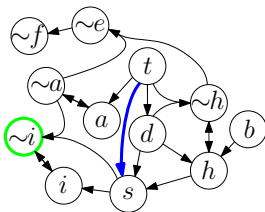
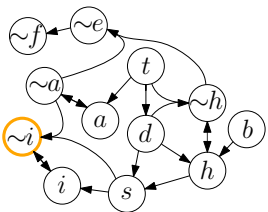
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Relevant updates

- **However, in many cases updates are not irrelevant.**
- An update is relevant whenever it causes the status of at least one literal to change.

Example (A relevant update)

Consider again \mathcal{P}_1 , where we have that $S_{\mathcal{P}_1}(s) = S_{\mathcal{P}_1}(t) = \text{IN}$. For update $u = +(s \leftarrow t)$, we have that $S_{u(\mathcal{P}_1)}(\sim i) = \text{IN}$, though it was UNDECIDED before performing the update. The change in the status of s is caused by the new argument $\langle \mathcal{A}_{10}, \sim i \rangle = \langle \{(\sim i \leftarrow \sim a, s)\}, \sim i \rangle$ for $u(\mathcal{P}_1)$ and \mathcal{A}_{10} is preferred to all the other arguments of the form $\langle \mathcal{A}, i \rangle$.



Influenced Set

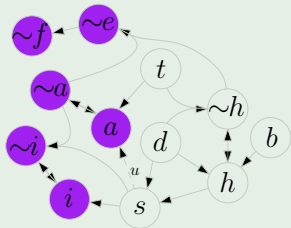
We propose the concept of *influenced set*, which consists of the literals that are reachable in $G(u, \mathcal{P})$ from the head of the rule r in the update u by using only the hyper-edges whose body does not contain an unreachable literal whose status is OUT.

Example (Influenced literals)

Consider the update $u = +(a \leftarrow s)$ over \mathcal{P}_1 , which yields the DeLP-program $u(\mathcal{P}_1)$. Thus, we have:

$\mathcal{R}(u, \mathcal{P}_1) = \{a, \sim a, i, \sim i, \sim e, \sim f\}$, and

$\mathcal{R}(u, \mathcal{P}_1) \supseteq \mathcal{I}(u, \mathcal{P}_1, \mathcal{S}_{\mathcal{P}_1}) = \{a, \sim a, i, \sim i\}$.



Influenced Set

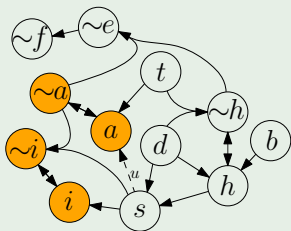
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Influenced Set: Definition

We propose the concept of *influenced set*, which consists of the literals that are reachable in $G(u, \mathcal{P})$ from the head of the rule r in the update u by using only the hyper-edges whose body does not contain an unreachable literal whose status is OUT.

Definition (Influenced Set)

Let \mathcal{P} be a DeLP-program, $u = \pm r$, and $S_{\mathcal{P}}$ the status of literals w.r.t. \mathcal{P} , and $G(u, \mathcal{P}) = \langle N^u, H^u \rangle$.

- $\mathcal{I}_0(u, \mathcal{P}, S_{\mathcal{P}}) = \begin{cases} \emptyset & \text{if } u \text{ is irrelevant for } \mathcal{P} \\ \{\text{head}(r)\} & \text{otherwise;} \end{cases}$
- $\mathcal{I}_{i+1}(u, \mathcal{P}, S_{\mathcal{P}}) = \mathcal{I}_i(u, \mathcal{P}, S_{\mathcal{P}}) \cup \{ \sim\alpha \mid \exists (\{\alpha\}, \sim\alpha) \in H^u \text{ s.t. } \alpha \in \mathcal{I}_i(u, \mathcal{P}, S_{\mathcal{P}}) \} \cup \{ y \mid \exists (X, \alpha) \in H^u \text{ s.t. } X \cap \mathcal{I}_i(u, \mathcal{P}, S_{\mathcal{P}}) \neq \emptyset \wedge X \cap \text{OUT}(u, \mathcal{P}, S_{\mathcal{P}}) = \emptyset \}$.

The *influenced set* for u w.r.t. \mathcal{P} and $S_{\mathcal{P}}$ is then defined as

$\mathcal{I}(u, \mathcal{P}, S_{\mathcal{P}}) = \mathcal{I}_n(u, \mathcal{P}, S_{\mathcal{P}})$ such that $\mathcal{I}_n(u, \mathcal{P}, S_{\mathcal{P}}) = \mathcal{I}_{n+1}(u, \mathcal{P}, S_{\mathcal{P}})$.

Inferable and Core Literals

[Inferable] The status of a literal for which there is no argument in the (updated) program may depend only on the status of its complementary literal—we call such literals *inferable*.

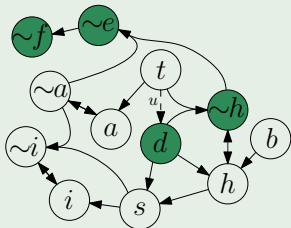
[Core] The core literals for a relevant update $u = \pm r$ w.r.t. \mathcal{P} are those in $Lit_{\mathcal{P}}$ that are influenced but are not inferable.

Example (Inferable and Core literals)

Consider the update $u = -(d \leftarrow t)$ over \mathcal{P}_1 , which yields the DeLP-program $u(\mathcal{P}_1)$. Thus, we have:

$$Infer(u, \mathcal{P}_1) = \{d, \sim h, \sim e, \sim f\}$$

$$Core(u, \mathcal{P}_1) = \{h, s, \sim i, i\}.$$



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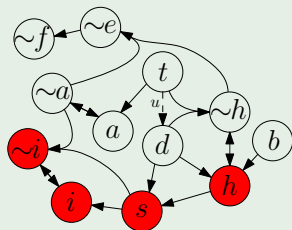
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Inferable and Core Literals: Definitions

The status of a literal for which there is no argument in the (updated) program may depend only on the status of its complementary literal—we call such literals *inferable*. Using the hyper-graph of updated programs, we can define inferable literals as follows.

Definition (Set of Inferable Literals)

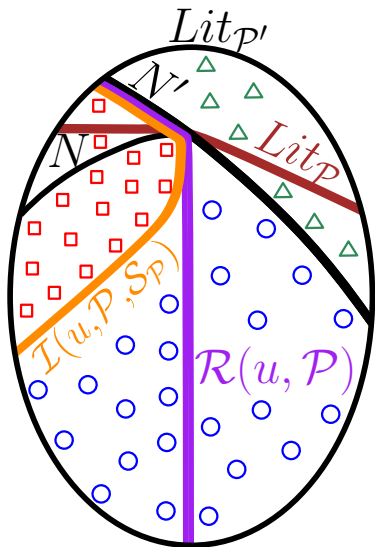
Let \mathcal{P} be a DeLP-program, $u = \pm r$, $\mathcal{P}' = u(\mathcal{P})$, and $G(\mathcal{P}') = \langle N', H' \rangle$. The set of inferable literals for u w.r.t. \mathcal{P} is $Infer(u, \mathcal{P}) = Lit_{\mathcal{P}'} \setminus N'$.

The core literals for a relevant update $u = \pm r$ w.r.t. \mathcal{P} are those in $Lit_{\mathcal{P}'}$ that are influenced but are not inferable.

Definition (Set of Core Literals)

Let \mathcal{P} be a DeLP-program, $u = \pm r$, and $S_{\mathcal{P}}$ the status of the literals of \mathcal{P} . The set $Core(u, \mathcal{P})$ of core literals for u w.r.t. \mathcal{P} is $Core(u, \mathcal{P}) = (I(u, \mathcal{P}, S_{\mathcal{P}}) \setminus Infer(u, \mathcal{P})) \cap Lit_{\mathcal{P}'}$.

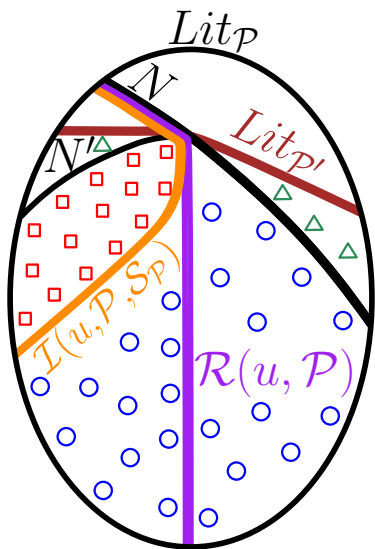
Relationships for addition



Legend :

○	PR
□	$Core(u, P)$
△	$Infer(u, P)$

Relationships for deletion



Legend :

○	PR
□	$Core(u, P)$
△	$Infer(u, P)$

Incremental Algorithm

Algorithm Dynamic DeLP-Solver

Input: DeLP-program \mathcal{P} , Initial status $S_{\mathcal{P}}$, Update $u = \pm r$.

Output: Status $S_{\mathcal{P}'}$ w.r.t. the updated program $\mathcal{P}' = u(\mathcal{P})$.

- 1: **if** one of Propositions 2–4 holds (the update is irrelevant) **then**
- 2: **return** $S_{\mathcal{P}}$; // Nothing changes
- 3: **if** $\{head(r), \sim head(r)\} \cap Lit_{\mathcal{P}} = \emptyset$ **then**
- 4: **return** $S_{\mathcal{P}} \cup \{(head(r), \text{DELP-SOLVER}(\mathcal{P}', head(r)))\}$; // New fresh literal
- 5: Let $G(\mathcal{P}') = \langle N', H' \rangle$; // Build the Hyper-Graph
- 6: Let $PR = \{\alpha \in N' \setminus \mathcal{I}(u, \mathcal{P}, S_{\mathcal{P}})\}$; // Preserved Literals
- 7: **for** $\alpha \in PR$ **do**
- 8: $S_{\mathcal{P}'}(\alpha) \leftarrow S_{\mathcal{P}}(\alpha)$; // Status Preserved
- 9: **for** $\alpha \in Core(u, \mathcal{P})$ **do**
- 10: $S_{\mathcal{P}'}(\alpha) \leftarrow \text{DELP-SOLVER}(\mathcal{P}', \alpha)$; // Status must be computed
- 11: **for** $\alpha \in Infer(u, \mathcal{P})$ **do**
- 12: **if** $S_{\mathcal{P}'}(\sim\alpha) = \text{IN}$
- 13: **then** $S_{\mathcal{P}'}(\alpha) \leftarrow \text{OUT}$ // Status Inferred
- 14: **else** $S_{\mathcal{P}'}(\alpha) \leftarrow \text{UNDECIDED}$; // Status Inferred
- 15: **for** $\alpha \in Lit \setminus Lit_{\mathcal{P}'}$ **do**
- 16: $S_{\mathcal{P}'}(\alpha) = \text{UNKNOWN}$ // Literal is not in the language of the updated program
- 17: **return** $S_{\mathcal{P}'}$.

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Dataset & Methodology

Datasets:

Inspired by the structure of the DeLP-program in our running example, we generated a set of 40 DeLP programs, each consisting of a number of literals in $\{180, 220\}$, of facts in $\{10, 20\}$, of strict rules in $\{20, 30\}$, and a number of defeasible rules in $\{100, 150\}$. For each program, we generated 5 different rule addition/deletion updates.

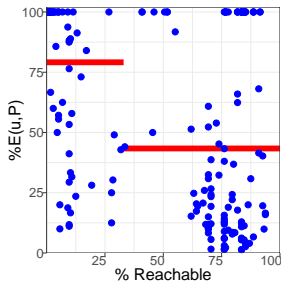
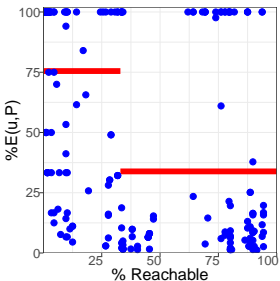
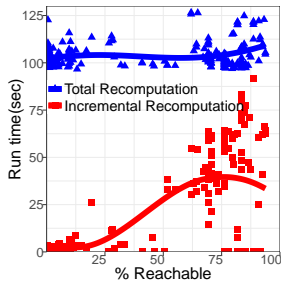
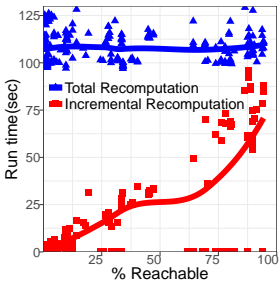
Methodology

[Efficiency] For each DeLP-program \mathcal{P} in the dataset, we compared the average running time of Algorithm 1 with that of the approach from scratch, which computes the status in the updated program by directly calling the DeLP-Solver for each literal of \mathcal{P} .

[Effectiveness] We also measured the percentage of literals whose status needs to be recomputed over the set of literals whose status is recomputed by Algorithm 1.

$$E(u, \mathcal{P}) = \frac{|Rec(u, \mathcal{P})|}{|Core(u, \mathcal{P}) \cup Infer(u, \mathcal{P})|}$$

Experimental Results for addition/deletion (left/right)



Results

- 1) We compared our technique with the computation from scratch.
- 2) We performed experiments that aimed at evaluating both the efficiency and effectiveness of our approach.
- 3) Our incremental algorithm outperforms the computation from scratch.
- 4) For almost half of the updates performed, the proposed technique computes only the status of literals whose status actually needs to be recomputed.

Outline

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 - Motivation
- 2 Background
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 - Dealing with Irrelevant Updates
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 - Our Technique
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- * We have taken the first steps in tackling the problem of avoiding wasted effort when determining the warrant status of literals in a DeLP program after that a (defeasible or strict) rule is added/removed.
- * Our incremental approach outperforms the computation from scratch (especially if the average number of literals reachable from an update is less than 33%).

FW1) Further developing these techniques, as well as developing similar ones for fact addition and deletion, and the more general case of simultaneously adding or deleting a *set* of rules and facts.

FW2) We believe the basic ideas in the framework could carry over to other frameworks, v.g. ASPIC+, ABA.

Thank you!

... any ~~question~~ **argument**?